# STUDY ON POLYCONDENSATION REACTIONS

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#### CERTIFICATE

This is to certify that present work "Study on polycondensation reactions" has been carried out under my supervision and this has not been submitted elsewhere for a degree.

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#### NOMENCLATURE

```
k<sub>1</sub>,k<sub>2</sub> = forward reaction rate constants.
k_1', k_2'
          = reverse reaction rate constants
          = time, sec.
cp,cq,
        = concentrations of P, Q, Z and V respectively
cz,cv
           = value of c_p and c_q in the main body of the liquid
           = value of \mathbf{c_v} at the phase boundary
           = diffusivity, cm<sup>2</sup>/sec.
D
 t
           = time increment
 x
           = space increment
           = molecular weight of propylene glycol
M_{G}
           = molecular weight of adipic acid
           = number average molecular weight
M.,
           = weight average molecular weight
           = poly dispersity index
PDI
```

#### ABSTRACT

This work consists of two parts. In the first part, firstly the kinetics of reversible step polymerisation is discussed. The MWD for the reversible reaction involving asymmetric monomers is predicted to be same as that for irreversible reaction, if it is assumed that in a given species all the internal arrangements are equally probable. Secondly, an algorithm developed by Vimala and Nath was used to solve linear simultaneous partial differential equations describing mass transfer accompanied by polycondensation. In the second part an experimental apparatus that has been set up to perform polycondensation reactions has been described. The samples were analysed for acid number, hydroxyl number, water content. The samples were also analysed for molecular weight distribution by GPC. The  $\overline{\mathbb{M}}_n$  calculated from acid and hydroxyl number is in good agreement with that calculated from theoretical considerations.

#### CHAPTER 1

#### INTRODUCTION

Several important polymers are produced by step polymerisation mechanism. In this type of polymerisation monomers with chemically reactive functional groups form the polymers. In the first part of this thesis, some theoretical work concerning reversible step polymerisation is presented. Firstly, molecular weight distribution in step polymerisation of two diffunctional monomers one of them possessing structural asymmetry is calculated. Secondly a numerical technique for solving two simultaneous linear partial differential equations which arise out of simultaneous diffusion and polycondensation reaction is presented. In the second part of the thesis an experimental apparatus designed for carrying out polycondensation reactions is described and results of some experiments performed are presented.

#### CHAPTER 2

### KINETICS OF REVERSIBLE STEP POLYMERISATION

Step polymers such as polyesters, polyurathanes, etc., can be considered as products of reaction between two diffunctional monomers. Such polymerisations have been analysed using Flory's equal reactivity hypothesis. However examples of monomers for which the equal reactivity assumption is invalid are plenty. Three types of such monomers are

- 1. Asymmetric monomers in which the groups are not chemically equivalent, for example, a glycol with a primary and secondary hydroxyl groups whose reactivities are different
- 2. Cyclic monomers such as anhydrides. Here the anhydride group generates a carboxyl group on reaction with a hydroxyl group but the reactivities of carboxyl and anhydride groups are different.
- 3. Monomers with induced symmetry. In such monomers the functional groups are equally reactive till one of them reacts.

Case 1 presented the molecular weight distribution (MWD) interms of the probabilities of reaction of functional groups. Gandhi and Babu 2 studied the effects of unequal

reactivity on the polymerisation kinetics and obtained these probabilities as functions of time for various values of the rate constants. In all of these studies, however, only irreversible reactions were studied. It is well known that Florysdistribution derived for irreversible equal reactivity case is also valid for reversible equal reactivity case.

Numerical computations by Somu<sup>3</sup> for reaction mixtures initially containing stoichiometrically equal amounts of reactants indicate that the MWD for reversible as well as irreversible polymerisations at the same conversion are identical. In this work, it is intended to provide a theoretical understanding of the above result for reversible polymerisation reactions for asymmetric monomers.

One common class of polymerisation which is often encountered is of the  $A_1A_2$  + BB type, where  $A_1$ ,  $A_2$  and B are functional groups with  $A_1$  and  $A_2$  groups reacting with B groups at different rates. This is classified as asymmetry and it also implies that the reactivities of both the functional groups  $A_1$  and  $A_2$  are unaffected by the length of the chain at the end of which they are present. For such polymerisation involving asymmetric monomers, all the possible reactions that can occur between the functional groups will be listed first. The various types of molecules present at any time are given in Table 1.

# Table 1 NOTATIONS

Type of species	Symbol used for representing species	Symbol used for representing concentration of species
<sup>A</sup> 1 <sup>A</sup> 2	(A <sub>1</sub> A <sub>2</sub> )	[442]
(BBA <sub>1</sub> A <sub>2</sub> ) <sub>n-1</sub> BB	(BB) <sub>n-1</sub>	[BB] n-1
(A <sub>1</sub> A <sub>2</sub> BB) <sub>n</sub> A <sub>1</sub> A <sub>2</sub>	$(A_1A_2)_n$	$[A_1A_2]_n$
(A <sub>1</sub> A <sub>2</sub> BB) <sub>n</sub> A <sub>2</sub> A <sub>1</sub>	$(A_1A_1)_n$	[A <sub>1</sub> A <sub>1</sub> ] <sub>n</sub>
(A2A1BB) <sub>n</sub> A1A2	$(A_2A_2)_n$	$[A_2A_2]_n$
(A1A2BB)n	$(A_1B)_n$	$[A_1B]_n$
$(A_2A_1BB)_n$	(A <sub>2</sub> B) <sub>n</sub>	[A <sub>2</sub> B] <sub>n</sub>
W	(W)	[ w ]

The reactions that can occur between the functional groups are as follows:

$$(A_1A_2) + (BB)_{m-1} = \frac{k_1}{k_1^*} (A_2B)_m + (W)$$

$$(A_1A_2) + (BB)_{m-1} = \frac{k_2}{k_2'} (A_1B)_m + (W)$$

$$(A_1A_2) + (A_1B)_m \xrightarrow{k_1} (A_1A_2)_m + (W)$$

$$(A_1A_2) + (A_1B)_m = \frac{k_2}{k_2^*} (A_1A_1)_m + (W)$$

$$(A_1A_2) + (A_2B)_m = \frac{k_1}{k_1^*} (A_2A_2)_m + (W)$$

$$(A_1A_2) + (A_2B)_m \xrightarrow{k_2} (A_1A_2)_m + (W)$$

$$(A_1A_2)_{n}^+$$
 (BB)<sub>m-1</sub>  $\frac{k_1}{k_1^*}$   $(A_2B)_{m+n}^+$  + (W)

$$(A_1A_2)_n + (BB)_{m-1} + (W)_{m+n} + (W)_{m+n}$$

$$(A_1A_1)_n + (BB)_{n-1} \xrightarrow{k_1} (A_1B)_{m+n} + (W)$$

$$(A_2A_2)_n + (BB)_{m-1} = \frac{k_2}{k_2'} (A_2B)_{m+n} + (W)$$

$$(A_1B)_n + (BB)_{m-1} \xrightarrow{k_1} (BB)_{m+n-1} + (W)$$

$$(A_2B)_n + (BB)_{m-1} \xrightarrow{k_2} (BB)_{m+n-1} + (W)$$

$$(A_1B)_n + (A_1A_2)_m \xrightarrow{k_1^*} (A_1A_2)_{m+n} + (W)$$

$$(A_1B)_n + (A_1A_2)_m \xrightarrow{k_2} (A_1A_1)_{m+n} + (W)$$

$$(A_2B)_n + (A_1A_2)_m = \frac{A_1}{k_1^*} (A_2A_2)_{m+n} + (W)$$

$$(A_2B)_n + (A_1A_2)_m = \frac{k_2}{k_2!} (A_1A_2)_{m+n} + (W)$$

$$(A_1B)_n + (A_1A_1)_m \xrightarrow{k_1} (A_1A_1)_{m+n} + (W)$$

$$(A_2B)_n + (A_1A_1)_m \xrightarrow{k_1} (A_1A_2)_{m+n} + (W)$$

$$(A_1B)_n + (A_2A_2)_m \xrightarrow{k_2} (A_1A_2)_{m+n} + (W)$$

$$(A_2B)_n + (A_2A_2)_m \xrightarrow{k_2} (A_2A_2)_{m+n} + (W)$$

$$(A_1B)_n + (A_1B)_m \xrightarrow{k_1} (A_1B)_{m+n} + (W)$$

$$(A_2B)_n + (A_2B)_m \xrightarrow{k_2} (A_2B)_{m+n} + (W)$$

$$(A_1B)_n + (A_2B)_m \xrightarrow{k_1} (A_2B)_{m+n} + (W)$$

$$(A_1B)_n + (A_2B)_m \xrightarrow{k_2} (A_1B)_{m+n} + (W)$$

In the above equations W is being used to symbolize a side product that might be formed. It is to be emphasised

that the same rate constant for a given group is used irrespective of the chain length. The rate expressions for the disappearance of these species can be written as follows:

$$-\frac{d \left[ A_{1} A_{2} \right]}{d t} = + 2k_{1} \left[ A_{1} A_{2} \right] \sum_{n=1}^{\infty} \left[ BB \right]_{n-1} \\
+ 2k_{2} \left[ A_{1} A_{2} \right] \sum_{n=1}^{\infty} \left[ BB \right]_{n-1} \\
+ k_{1} \left[ A_{1} A_{2} \right] \sum_{n=1}^{\infty} \left[ A_{1} B \right]_{n} \\
+ k_{2} \left[ A_{1} A_{2} \right] \sum_{n=1}^{\infty} \left[ A_{2} B \right]_{n} \\
+ k_{1} \left[ A_{1} A_{2} \right] \sum_{n=1}^{\infty} \left[ A_{2} B \right]_{n} \\
+ k_{2} \left[ A_{1} A_{2} \right] \sum_{n=1}^{\infty} \left[ A_{2} B \right]_{n} \\
- k_{1}^{\prime} \left[ W \right] \sum_{m=1}^{\infty} \left[ A_{1} B \right]_{m} \\
- k_{2}^{\prime} \left[ W \right] \sum_{m=1}^{\infty} \left[ A_{1} A_{2} \right]_{m} \\
- k_{1}^{\prime} \left[ W \right] \sum_{m=1}^{\infty} \left[ A_{1} A_{1} \right]_{m} \\
- 2k_{1}^{\prime} \left[ W \right] \sum_{m=1}^{\infty} \left[ A_{1} A_{2} \right]_{m} \\
- 2k_{1}^{\prime} \left[ W \right] \sum_{m=1}^{\infty} \left[ A_{1} A_{2} \right]_{m} \\
- k_{2}^{\prime} \left[ W \right] \sum_{m=1}^{\infty} \left[ A_{1} A_{2} \right]_{m} \\
- k_{2}^{\prime} \left[ W \right] \sum_{m=1}^{\infty} \left[ A_{1} A_{2} \right]_{m}$$

$$(2.1)$$

$$-\frac{d[BB]}{dt}_{n-1} = + 2k_{1} [BB]_{n-1} [A_{1}A_{2}]$$

$$+ 2k_{2} [BB]_{n-1} [A_{1}A_{2}]$$

$$+ 2k_{1} [BB]_{n-1} \sum_{m=1}^{\infty} [A_{1}A_{2}]_{m}$$

$$+ 2k_{2} [BB]_{n-1} \sum_{m=1}^{\infty} [A_{1}A_{2}]_{m}$$

$$+ 4k_{1} [BB]_{n-1} \sum_{m=1}^{\infty} [A_{1}A_{1}]_{m}$$

$$+ 4k_{2} [BB]_{n-1} \sum_{m=1}^{\infty} [A_{2}A_{2}]_{m}$$

$$+ 2k_{1} [BB]_{n-1} \sum_{m=1}^{\infty} [A_{2}B]_{m}$$

$$+ 2k_{2} [BB]_{n-1} \sum_{m=1}^{\infty} [A_{2}B]_{m}$$

$$+ (k_{1}^{*} + k_{2}^{*}) [W] (n-1) [BB]_{n-1}$$

$$- k_{1}^{*} [W] [A_{2}B]_{n}$$

$$- k_{2}^{*} [W] [A_{1}B]_{n}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [A_{1}B]_{m}$$

$$-\frac{k'_{1}}{2} [W] \sum_{m=n+1}^{\infty} [A_{1}B]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [A_{2}B]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n}^{\infty} [BB]_{m}$$

$$-\frac{k'_{1}}{2} [W] \sum_{m=n}^{\infty} [BB]_{m}$$

$$-\frac{k'_{1}}{2} [W] \sum_{m=n}^{\infty} [BB]_{m}$$

$$-\frac{k'_{1}}{2} [W] \sum_{m=n}^{\infty} [BB]_{m}$$

$$-\frac{k'_{1}}{2} [W] \sum_{m=n}^{\infty} [BB]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n}^{\infty} [BB]_{m}$$

$$-\frac{k'_{1}}{2} [W] \sum_{m=n}^{\infty} [BB]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [BB]_{m}$$

$$-\frac{k'_{1}}{2} [W] \sum_{m=n+1}^{\infty} [BB]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [A_{2}B]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [BB]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [A_{2}B]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [A_{2}B]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [A_{2}B]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [BB]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [A_{2}B]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [BB]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [BB]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [A_{2}B]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [A_{2}B]_{m}$$

$$-\frac{k'_{2}}{2} [W] \sum_{m=n+1}^{\infty} [A_{2}B]_{m}$$

$$\frac{-d[A_{1}A_{2}]_{n}}{dt} = + 2k_{1}[A_{1}A_{2}]_{n} \sum_{m=1}^{\infty} [BB]_{m-1}$$

$$+ 2k_{2}[A_{1}A_{2}]_{n} \sum_{m=1}^{\infty} [BB]_{m-1}$$

$$+ k_{1}[A_{1}A_{2}]_{n} \sum_{m=1}^{\infty} [A_{1}B]_{m}$$

$$+ k_{2}[A_{1}A_{2}]_{n} \sum_{m=1}^{\infty} [A_{1}B]_{m}$$

.

$$+ k_1 \begin{bmatrix} A_1 A_2 \end{bmatrix} \sum_{m=1}^{\infty} [A_2 B]_m$$

$$+ k_2 [A_1A_2] \sum_{m=1}^{\infty} [A_2B]_m$$

+ 
$$(k_1 + k_2) n [W] [A_1 A_2]_n$$

$$-\frac{k_1^{\prime}}{2} \left[ w \right] \sum_{m=n+1}^{\infty} \left[ A_2 B \right]_{m}$$

$$-\frac{k!}{2} [W] \sum_{m=n+1}^{\infty} [A_1B]_m$$

$$-\frac{\mathbf{k}_{1}^{\prime}}{2} \left[\mathbf{W}\right] \sum_{\mathbf{m}=\mathbf{n}+1}^{\infty} \left[\mathbf{A}_{1}\mathbf{A}_{2}\right]_{\mathbf{m}}$$

$$- k_{2}^{\prime} \left[ w \right] \sum_{m=n+1}^{\infty} \left[ A_{1} A_{1} \right]_{m}$$

- 
$$k$$
;  $[W] \sum_{m=n+1}^{\infty} [A_2A_2]_m$ 

$$- k_2' [W] \sum_{m=n+1}^{\infty} [A_1 A_2]_m$$

$$-k_1[A_1A_2][A_1B]_n$$

$$- k_2[A_1A_2][A_2B]_n$$

$$-k_1 \sum_{m=1}^{n-1} [A_1 A_2]_{n-m} [A_1 B]_m$$

$$-k_{2} \sum_{m=1}^{n-1} [A_{1}A_{2}]_{n-m} [A_{2}B]_{m}$$

$$-2k_{1} \sum_{m=1}^{n-1} [A_{1}A_{1}]_{n-m} [A_{2}B]_{m}$$

$$-2k_{2} \sum_{m=1}^{n-1} [A_{2}A_{2}]_{n-m} [A_{1}B]_{m} \qquad (2.3)$$

$$\frac{-d \left[A_{1}A_{1}\right] n}{dt} = + 2k_{1} \left[A_{1}A_{1}\right]_{n} \sum_{m=1}^{\infty} \left[A_{1}B\right]_{m} 
+ 2k_{1} \left[A_{1}A_{1}\right]_{n} \sum_{m=1}^{\infty} \left[A_{2}B\right]_{m} 
+ 4k_{1} \left[A_{1}A_{1}\right]_{n} \sum_{m=1}^{\infty} \left[BB\right]_{m-1} 
+ k'_{2}(n+1) \left[W\right] \left[A_{1}A_{1}\right]_{n} 
+ k'_{1}(n-1) \left[W\right] \left[A_{1}A_{1}\right]_{n} 
- k'_{1} \left[W\right] \sum_{m=n+1}^{\infty} \left[A_{1}B\right]_{m} 
- k'_{1} \left[W\right] \sum_{m=n+1}^{\infty} \left[A_{1}A_{2}\right]_{m} 
- k'_{1} \left[W\right] \sum_{m=n+1}^{\infty} \left[A_{1}A_{1}\right]_{m}$$

$$- k_{2} \begin{bmatrix} A_{1}A_{2} \end{bmatrix} \begin{bmatrix} A_{1}B \end{bmatrix}_{n}$$

$$- k_{2} \sum_{m=1}^{n-1} \begin{bmatrix} A_{1}A_{2} \end{bmatrix}_{n-m} \begin{bmatrix} A_{1}B \end{bmatrix}_{m}$$

$$- 2k_{1} \sum_{m=1}^{n-1} \begin{bmatrix} A_{1}A_{1} \end{bmatrix}_{n-m} \begin{bmatrix} A_{1}B \end{bmatrix}_{m}$$
(2.4)

$$\frac{-d \left[A_{2}A_{2}\right] n}{dt} = + 4k_{2} \left[A_{2}A_{2}\right] n \sum_{m=1}^{\infty} \left[BB\right]_{m-1} \\
+ 2k_{2} \left[A_{2}A_{2}\right] n \sum_{m=1}^{\infty} \left[A_{2}B\right]_{m} \\
+ 2k_{2} \left[A_{2}A_{2}\right] n \sum_{m=1}^{\infty} \left[A_{1}B\right]_{m} \\
+ k_{1}^{\prime} (n+1) \left[W\right] \left[A_{2}A_{2}\right] n \\
+ k_{2}^{\prime} (n-1) \left[W\right] \left[A_{2}A_{2}\right] n \\
- \frac{k_{2}^{\prime}}{2} \left[W\right] \sum_{m=n+1}^{\infty} \left[A_{2}B\right] m \\
- \frac{k_{2}^{\prime}}{2} \left[W\right] \sum_{m=n+1}^{\infty} \left[A_{2}A_{2}\right] m \\
- k_{2}^{\prime} \left[W\right] \sum_{m=n+1}^{\infty} \left[A_{2}A_{2}\right] m$$

$$- k_{1} \begin{bmatrix} A_{1}A_{2} \end{bmatrix} \begin{bmatrix} A_{2}B \end{bmatrix}_{n}$$

$$- 2k_{2} \sum_{m=1}^{n-1} \begin{bmatrix} A_{2}A_{2} \end{bmatrix}_{n-m} \begin{bmatrix} A_{2}B \end{bmatrix}_{m}$$

$$- k_{1} \sum_{m=1}^{n-1} \begin{bmatrix} A_{1}A_{2} \end{bmatrix}_{n-m} \begin{bmatrix} A_{2}B \end{bmatrix}_{m}$$

$$- k_{1} \sum_{m=1}^{n-1} \begin{bmatrix} A_{1}A_{2} \end{bmatrix} \begin{bmatrix} A_{1}B \end{bmatrix}_{n}$$

$$+ k_{1} \begin{bmatrix} A_{1}A_{2} \end{bmatrix} \begin{bmatrix} A_{1}B \end{bmatrix}_{n}$$

$$+ k_{2} \begin{bmatrix} A_{1}A_{2} \end{bmatrix} \begin{bmatrix} A_{1}B \end{bmatrix}_{n}$$

$$+ 2k_{1} \begin{bmatrix} A_{1}B \end{bmatrix}_{n} \sum_{m=1}^{\infty} \begin{bmatrix} A_{1}A_{2} \end{bmatrix}_{m}$$

$$+ k_{2} \begin{bmatrix} A_{1}B \end{bmatrix}_{n} \sum_{m=1}^{\infty} \begin{bmatrix} A_{1}A_{2} \end{bmatrix}_{m}$$

$$+ 2k_{1} \begin{bmatrix} A_{1}B \end{bmatrix}_{n} \sum_{m=1}^{\infty} \begin{bmatrix} A_{1}A_{1} \end{bmatrix}_{m}$$

$$+ 2k_{2} \begin{bmatrix} A_{1}B \end{bmatrix}_{n} \sum_{m=1}^{\infty} \begin{bmatrix} A_{1}A_{1} \end{bmatrix}_{m}$$

$$+ 2k_{2} \begin{bmatrix} A_{1}B \end{bmatrix}_{n} \sum_{m=1}^{\infty} \begin{bmatrix} A_{2}A_{2} \end{bmatrix}_{m}$$

$$+ 2k_{1} \begin{bmatrix} A_{1}B \end{bmatrix}_{n} \sum_{m=1}^{\infty} \begin{bmatrix} A_{2}A_{2} \end{bmatrix}_{m}$$

$$+ 2k_{1} \begin{bmatrix} A_{1}B \end{bmatrix}_{n} \sum_{m=1}^{\infty} \begin{bmatrix} A_{2}B \end{bmatrix}_{m}$$

$$+ k_{1} \begin{bmatrix} A_{1}B \end{bmatrix}_{n} \sum_{m=1}^{\infty} \begin{bmatrix} A_{2}B \end{bmatrix}_{m}$$

$$+ k_2 [A_1B]_n \sum_{m=1}^{\infty} [A_2B]_m$$

$$- k_1 [W] \sum_{m=n}^{\infty} [BB]_m$$

$$-\frac{\mathbf{k}_{1}^{\prime}}{2} \left[\mathbf{W}\right] \sum_{\mathbf{m}=n+1}^{\infty} \left[\mathbf{A}_{1}^{\mathbf{A}_{2}}\right]_{\mathbf{m}}$$

$$-k_2'$$
 [W]  $\sum_{m=n+1}^{\infty} [A_1A_1]_m$ 

$$-k_1^*[W] \sum_{m=n+1}^{\infty} [A_1A_1]_m$$

$$-\frac{k_{2}^{\prime}}{2}\left[W\right]\sum_{m=n+1}^{\infty}\left[A_{1}A_{2}\right]_{m}$$

$$-k_1'[W] \sum_{m=n+1}^{\infty} [A_1B]_m$$

$$-\frac{k_2'}{2} [w] \sum_{m=n+1}^{\infty} [A_2B]_m$$

$$- k_{2}^{\prime} [W] \sum_{m=n+1}^{\infty} [A_{1}B]_{m}$$

$$- k_{2} [A_{1}A_{2}] [BB]_{n-1}$$

$$- 2k_{2} \sum_{m=1}^{n} [BB]_{n-m} [A_{1}A_{2}]_{m-1}$$

$$- 4k_{1} \sum_{m=1}^{n} [BB]_{n-m} [A_{1}A_{1}]_{m-1}$$

$$- 2k_{1} \sum_{m=1}^{n-1} [A_{1}B]_{n-m} [A_{1}B]_{m}$$

$$- k_{2} \sum_{m=1}^{\infty} [A_{1}B]_{n-m} [A_{2}B]_{m}$$

$$- k_{2} \sum_{m=1}^{\infty} [A_{1}A_{2}] [A_{2}B]_{n}$$

$$+ k_{2} [A_{1}A_{2}] [A_{2}B]_{n}$$

$$+ 2k_{2} [A_{2}B]_{n} \sum_{m=1}^{\infty} [A_{1}A_{2}]_{m}$$

$$+ k_{2} [A_{2}B]_{n} \sum_{m=1}^{\infty} [A_{1}A_{2}]_{m}$$

$$+ k_{2} [A_{2}B]_{n} \sum_{m=1}^{\infty} [A_{1}A_{2}]_{m}$$

$$+ 2k_{1} [A_{2}B]_{n} \sum_{m=1}^{\infty} [A_{1}A_{2}]_{m}$$

$$+ 2k_{1} [A_{2}B]_{n} \sum_{m=1}^{\infty} [A_{1}A_{2}]_{m}$$

$$+ 2k_{2} [A_{2}B]_{n} \sum_{m=1}^{\infty} [A_{2}A_{2}]_{m}$$

$$+ 2k_{2} [A_{2}B]_{n} \sum_{m=1}^{\infty} [A_{2}B]_{m}$$

$$+ k_{1} [A_{2}B]_{n} \sum_{m=1}^{\infty} [A_{1}B]_{m}$$

$$+ k_{2} [A_{2}B]_{n} \sum_{m=1}^{\infty} [A_{1}B]_{m}$$

$$+ k_{1}^{2} [A_{2}B]_{n} \sum_{m=1}^{\infty} [A_{1}B]_{m}$$

$$+ k_{1}^{2} [M][A_{2}B]_{n}$$

$$+ k_{2}^{2} [M][A_{1}A_{2}]_{n}$$

$$- k_{2}^{2} [M][A_{2}A_{2}]_{n}$$

$$- k_{1}^{2} [M] \sum_{m=n+1}^{\infty} [A_{2}A_{2}]_{m}$$

$$- k_{1}^{2} [M] \sum_{m=n+1}^{\infty} [A_{1}A_{2}]_{m}$$

$$- k_{2}^{2} [M] \sum_{m=n+1}^{\infty} [A_{1}A_{2}]_{m}$$

$$- k_{2}^{2} [M] \sum_{m=n+1}^{\infty} [A_{1}A_{2}]_{m}$$

$$- k_{2}^{2} [M] \sum_{m=n+1}^{\infty} [A_{1}A_{2}]_{m}$$

$$- k_{2}^{*} [W] \sum_{m=n+1}^{\infty} [A_{2}A_{2}]_{m}$$

$$- k_{2}^{*} [W] \sum_{m=n+1}^{\infty} [A_{2}B]_{m}$$

$$- k_{1}^{*} [W] \sum_{m=n+1}^{\infty} [A_{2}B]_{m}$$

$$- k_{2}^{*} [W] \sum_{m=n+1}^{\infty} [A_{1}B]_{m}$$

$$- k_{1}^{*} [A_{1}A_{2}][BB]_{n-1}$$

$$- k_{1}^{*} \sum_{m=1}^{n} [BB]_{n-m} [A_{1}A_{2}]_{m-1}$$

$$- 4k_{2} \sum_{m=1}^{n} [BB]_{n-m} [A_{2}A_{2}]_{m-1}$$

$$- 2k_{2} \sum_{m=1}^{n} [A_{2}B]_{n-m} [A_{2}B]_{m}$$

$$- k_{1} \sum_{m=1}^{n-1} [A_{2}B]_{n-m} [A_{1}B]_{m}$$

$$(2.7)$$

In deriving the above equations care has to be taken to account for chain breakage due to reverse reaction which can occur at two places and produce the same product. For example,  $(A_2A_1)_n$  can produce  $A_1A_2$  monomer by reverse reaction in two ways. In the above derivation one assumption was used. The symbol adopted for all the species do not

reflect all the internal arrangements. For example,  $(A_1^B)_2$  actually consists of two types of molecules;  $A_1^A_2^BBA_1^A_2^BB$  and  $A_1^A_2^BBA_1^A_2^BB$ . It was assumed that both the species are equally probable in occurrence. This also implies that in a complicated molecule such as  $(A_2A_1)_n$  probabilities of occurrence of  $(A_1A_2BB)_mA_1A_2$   $(BBA_1A_2)_{n-m}$  and  $(A_1A_2BB)_mA_2A_1$   $(BBA_1A_2)_n$  are equal. Following the strong suggestion from Somu's work, it is now intended to test whether the M.W.D. predicted for irreversible reactions is valid for the reversible reactions as well.

Let  $\alpha$ ,  $\beta$  and  $\gamma$  respectively represent the fraction of initial B,A, and A, groups that have reacted at any time. Then from stoichiometry

$$\alpha = \frac{R(\beta + \gamma)}{2} \tag{2.8}$$

where  $R = \frac{\left[A\right]_{O}}{\left[B\right]_{O}}$ . Here the initial group concentration of both  $A_{1}$  and  $A_{2}$  is equal to  $\left[A\right]_{O}$ . Then Case's results on MWD for the irreversible polymerisation involving asymmetric monomer can be rearranged to give the following:

$$(BB)_{n-1} = B_0 (1-\alpha)^2 (R\beta\gamma)^{n-1}$$

$$(A_1B)_n = RB_0 (1-\beta) (1-\alpha)\gamma (R\beta\gamma)^{n-1}$$

$$(A_2B)_n = RB_0 (1-\alpha) (1-\gamma)\beta (R\beta\gamma)^{n-1}$$

$$(A_1 A_1)_n = R^2 B_0 (1-\beta)^2 \gamma^2 (R \beta \gamma)^{n-1}$$

$$(A_2 A_2)_n = R^2 B_0 (1-\gamma)^2 \beta^2 (R \beta \gamma)^{n-1}$$

$$(A_1 A_2)_n = R^2 B_0 (1-\beta) (1-\gamma) \beta \gamma (R \beta \gamma)^{n-1}$$

$$(A_1 A_2)_n = R^2 B_0 (1-\beta) (1-\gamma) (2.9)$$

If the unreacted  $\mathbb{A}_1$  group concentration is  $[\mathbb{A}_1]$ , the initial  $\mathbb{A}_1$  group concentration is  $[\mathbb{A}]_0$  and the unreacted  $\mathbb{B}$  group concentration is  $[\mathbb{B}]$  then intutively one would expect the over all rate equation for  $[\mathbb{A}_1]$  to be

$$-\frac{a[A_1]}{dt} = k_1[A_1][B] - k_1[W][A]_0 - [A_1]$$

similar equations might also be expected for unreacted  $\frac{1}{2}$  and B group concentrations. As a justification for the assumption made in deriving equations (2.1) to (2.7), it can be said that the above intutive expressions can be obtained from equations (2.1) to (2.7) by observing that

$$[A_1] = [A_1A_2] + \sum_{n=1}^{\infty} 2[A_1A_1]_n + \sum_{n=1}^{\infty} [A_1B]_n + \sum_{n=1}^{\infty} [A_1A_2]_n$$

and summing the appropriate rate equations. As a consequence,

the relationship between  $\,\beta\,$  and  $\,\gamma\,$  given by Gandhi and Babu<sup>2</sup>

$$(1-\beta)^{k_2} = (1-\gamma)^{k_1}$$
 (2.10)

is also valid.

If (2.4) is a solution to equations (2.1) to (2.7), then substitution of (2.9) into the LHS and RHS of any one of equations (2.1) to (2.7) must all yield the same equation. If equation (2.9) is substituted in equation (2.1) with the help of equations (2.8) and (2.10), equation (2.1) after subsequent mathematical simplification is reduced to give

$$\frac{d\beta}{dt} = 2 k_1 B_0 (1-\alpha)(1-\beta) - k_1' [W]\beta$$

Further when equation (2.9) is substituted in any of the rate expressions (2.2) to (2.7) and after use of equation (2.8) and (2.10) the same result is obtained. So the MWD predicted for asymmetric monomers in the case of irreversible reaction is also valid for reversible case.

Thus it can be concluded that if one assumes that in a given species all internal arrangements are equally probable, the MWD for reversible as well as irreversible step polymerisations with unequal reactivities are identical at a given conversion.

#### CHAPTER 3

### SIMULTANEOUS DIFFUSION AND POLYCONDENSATION

For several polycondensation processes the rate of conversion is not only determined by the chemical reaction rate, but also by the rate of removal of the volatile byproduct. Combination of mass transfer and chemical reaction have been studied in the case of gas absorption. The same methods may be used for polycondensation reactions. In the initial stages, the volatile product is easily removed. As the degree of polymerisation increases, the desorption rate is more important. Finally when chemical equilibrium is reached, the rate of conversion becomes equal to the shift of equilibrium composition with time and largely depends on the rate of mass transfer. It is for this later stage of polycondensation process that theoretical equations are obtained for the rate of interphase mass transfer accompanied by chemical reaction. The reaction for a polycondensation process can be written as

$$P + Q \longrightarrow Z + V$$

in which P and Q are reacting end groups, Z is the resulting ester group and V is the volatile component produced. For unsteady diffusion accompanied by reaction or for application

of penetration model, the following differential equation is valid for the concentration of volatile component.

$$\frac{\partial C_{V}}{\partial t} = D \frac{\partial^{2} C_{V}}{\partial x^{2}} + k_{c} (C_{p} C_{q} - \frac{C_{V} C_{Z}}{K_{C}})$$
 (3.1)

where  $\mathbf{k}_{_{\mathbf{C}}}$  is the condensation rate constant and  $\mathbf{K}_{_{\mathbf{C}}}$  is the equilibrium constant. The above nonlinear equation can be transformed into a first order system. The linearisation is made by assuming that deviations from mean concentration are small due to short contact times compared with the time necessary to produce a significant difference in the mean values of the concentrations of non-volatile component. So the deviation from equilibrium is small. Such a procedure has been suggested by Van Krevelen4. Following his work, the polycondensation reaction is now written as quasi firstorder reaction.

The concentrations  ${\tt C}_{{\tt A}}$  and  ${\tt C}_{{\tt B}}$  are defined as the distance from the equilibrium for V and P. The transformation is thus performed by introducing

$$c_{A} = c_{V} - \frac{\overline{c}_{p} \overline{c}_{q} K_{c}}{\overline{c}_{z}}$$

$$c_{B} = c_{p} - \overline{c}_{p}$$

$$k = \frac{k_{c} \overline{c}_{z}}{K_{c}} ; K = \frac{\overline{c}_{z}}{\overline{c}_{p}} K_{c}$$
(3.2)

and

in which  $c_V$  and  $c_p$  are the local concentrations of V and P and  $\overline{c}_p$  ,  $\overline{c}_q$  and  $\overline{c}_z$  are mean concentrations in the bulk of the liquid.

With the help of equation (3.2), equation (3.1) can be transformed to

$$\frac{\partial c_A}{\partial t} = D \frac{\partial^2 c_A}{\partial x^2} - k (c_A - c_B/K) \qquad (3.3)$$

In the same way, one can write

$$\frac{\partial^{C_{B}}}{\partial t} = D \frac{\partial^{2C_{B}}}{\partial x^{2}} + k (C_{A} - C_{B}/K)$$
 (3.4)

Initial conditions: at t=0, 
$$C_A = 0$$
;  $C_B = 0$  (3.5)

Boundary conditions: at t>0, x = 0,  $C_A = C_{AO}$  ( $C_V = C_{Vi}$ )

$$\frac{\partial x}{\partial c_B} = 0 \tag{3.6}$$

at t>0, 
$$x = \infty$$
,  $C_A = 0$ ,  $C_B = 0$  (3.7)

The initial condition is a state of equilibrium throughout the liquid. Desorption of component V starts at t=0. The B.C.(3.6) defines a quantity  $C_{\rm Vi}$  being the value of  $C_{\rm V}$  at the phase boundary in equilibrium with the vapour phase and also means that P can not desorbed. The B.C. (3.7) means that far away from the phase boundary chemical equilibrium

exists. The instantaneous supply rate per unit surface area,  $N_{\text{A}}$ , is given by

$$t_1 N_A = \int_0^\infty c_A dx + \int_0^\infty c_B dx$$

Mathematical computation:

A numerical solution of equations (3.3) and (3.4) subject to I.C.(3.5) and B.C.(3.6) and (3.7) is obtained by converting them into a set of implicit finite difference equations and solving the tridiagonal matrix equation on a computer by making use of a suitable algorithm.

Equations (3.3) and (3.4) are non-dimensionalised by using the following variables.

$$a = \frac{C_A}{C_{AO}}$$
;  $b = \frac{C_B}{C_{BO}}$ ;  $T = kt$ ;  $X = x\sqrt{\frac{k}{D}}$ 

to give

$$\frac{\partial a}{\partial t} = \frac{\partial^2 a}{\partial x^2} - (a - b/K)$$

$$\frac{\partial b}{\partial t} = \frac{\partial^2 b}{\partial x^2} + (a - b/K)$$
(3.8)

Now the I.C. : at 
$$T=0$$
,  $a=0$ ;  $b=0$ 

$$B.C. \rightarrow at T>0, X=0, a=1; \frac{\delta b}{\delta X}=0$$
at  $T>0, X=\infty$ ,  $a=0$ ;  $b=0$ 

When equation (3.8) is written in forward finite difference, it leads to

$$\frac{a_{n,m+1} - a_{n,m}}{\triangle T} = \frac{a_{n-1,m+1} - 2 a_{n,m+1}}{\triangle X^{2}} - (a_{n,m+1} - b_{n,m+1}/K)$$

$$\frac{b_{n,m+1}-b_{n,m}}{\triangle T} = \frac{b_{n-1,m+1}-2b_{n,m+1}+b_{n+1,m+1}}{\triangle X^2} + (a_{n,m+1}-b_{n,m+1}/a_{n,m+1})$$

which in turn written in matrix form gives

$$\begin{bmatrix} -\frac{1}{\Delta X^2} & 0 \\ c & -\frac{1}{\Delta X^2} \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix}_{n-1,m+1} + \begin{bmatrix} \frac{1}{\Delta T} + \frac{2}{\Delta X^2} + 1 & -\frac{1}{K} \\ -1 & \frac{1}{\Delta T} + \frac{2}{\Delta X^2} + \frac{1}{K} \end{bmatrix}$$

$$\begin{bmatrix} a \\ b \end{bmatrix}_{n,m+1} + \begin{bmatrix} -\frac{1}{\Delta x^2} & 0 \\ 0 & -\frac{1}{\Delta x^2} \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix}_{n+1,m+1} = \begin{bmatrix} \frac{a}{\Delta T} \\ \frac{b}{\Delta T} \end{bmatrix}_{n,m}$$

This can be rewritten in a convenient form

$$A_{n}W_{n-1} + B_{n}W_{n} + C_{n}W_{n+1} = D_{n}$$
 (3.9)

It may be noted that  $D_n$  is at a time level m where as all  $\tilde{W}$ 's are at an advanced time level m+1. The matrices  $A_n$ ,  $B_n$  and  $C_n$  are constant and known. An algorithm given by Vimala and Nath  $^5$  can be used to obtain the solution  $W_n$  at m+1:

$$W_n = - E_n W_{n+1} + J_n$$
  $1 \le n \le N-1$  (3.10)

where

$$E_{n} = (B_{n} - A_{n}E_{n-1})^{-1} C_{n}$$

$$J_{n} = (B_{n} - A_{n}E_{n-1})^{-1} (D_{n} - A_{n}J_{n-1})$$

$$2 \le n \le N-1$$

$$(3.11)$$
Using B.C;  $E_{1} = -\begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$ ;  $E_{N} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$ 

$$J_{1} = \begin{bmatrix} 1 \\ 0 \end{bmatrix} ; J_{N} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$
 (3.12)

By equations (3.10) and (3.12) 
$$W_{N} = \begin{bmatrix} 0 \\ Q \end{bmatrix}$$
 and by I.C  $W_{1} = \begin{bmatrix} 0 \\ Q \end{bmatrix}$ 

Knowing the values of dependent variables at m,i.e. corresponding to T, the dependent variable  $W_n$  at m+1, i.e. at T + $\Delta$ T can be computed by adopting the following procedure.

First, the values of matrix elements  $A_{11}$ ,  $B_{11}$ ...etc. are evaluated. Next with the help of equations (3.11) and (3.12)  $E_n$  and  $J_n$  based on the value of the variables at m are calculated for all n between 1 and N, starting from n = 1 and proceeding to n = N. By substituting the values of  $E_n$  and  $J_n$  in (3.10) and using B.C.(3.12), the values of the dependent variables  $W_n$  at m+1 are then determined in the reverse order i.e. starting from n =N. The so obtained values of  $W_n$  at m+1 can then be used to obtain  $W_n$  at m+2 and so on. The mass transfer rate was evaluated in terms of dimensionless groups appearing in the proposed equation

$$\frac{\overline{N}_{\Lambda}}{[\Lambda] \sqrt{Dk}} = \frac{1}{T_1} \left[ \int_{0}^{\infty} a \, dx + \int_{0}^{\infty} b \, dx \right]$$

The mass transfer rate is evaluated for various values of equilibrium constant. This has been plotted against T, with the equilibrium constant K as parameter in figure 1. Sherwood and Pigford<sup>6</sup> presented an analytical solution for the problem. It can be observed that the algorithm given by Vimla and Nath<sup>5</sup> is satisfactory. It was intended to apply this algorithm to convective mass transfer but could not be completed.

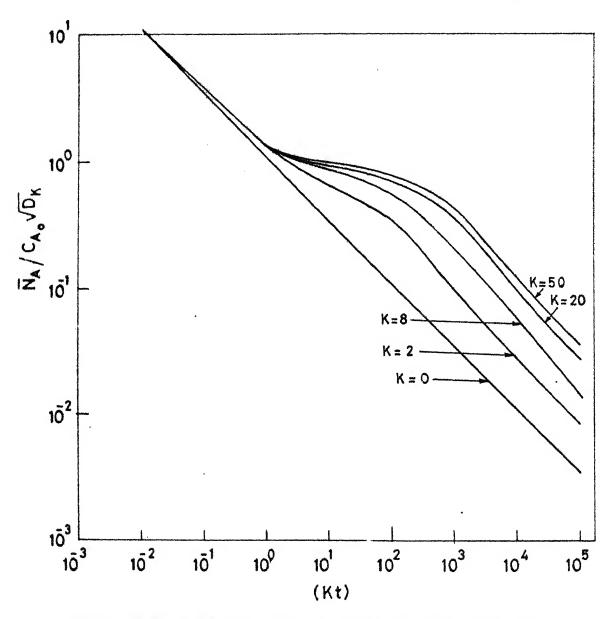


Fig.1. Effect of polycondensation on the rate of mass transfer

### CHAPTER 4

## EXPERIMENTAL WORK

Polycondensation is a process of obtaining high molecular weight compounds. This process is generally accompanied by the simultaneous elimination of some low molecular weight by product. Polycondensations are reversible and can reach an equilibrium. The establishment of the equilibrium is determined by the conditions of the condensation. Inorder to obtain polyesters with a high molecular weight it is necessary to select conditions ensuring the displacement of the equilibrium in the direction of the formation of the polyester molecule. This can be achieved only with the maximum elimination of low molecular weight by products from the reaction. So polycondensation is generally performed in two stages. First the reaction mixture is heated in a current of nitrogen as to ensure an inert atmosphere which prevents the degradation of higher molecular weight components and facilitates the elimination of low molecular weight reaction products from the reaction medium. In the second stage heating is continued in vacuum to eliminate the low molecular weight by products more completely. It was the aim of the experimental work to setup an apparatus where polycondensation reactions could be studied experimentally.

# Apparatus:

A cylindrical glass reactor of two litre capacity with a flange was used for carrying out the condensation polymerisation. In order to cover the reactor, a S.S. plate of diameter slightly bigger than that of the reactor was made. Threads were cut at the centre so that a bush could be fixed. In the bush a hole of diameter almost equal to that of stirre rod was made. A bearing was inserted on the top of the bush inorder to allow free rotation of the stirrer. The sketch of the reactor is shown in Figure 2. Care was taken to avoid leaks by fixing the bearing tightly. Three more holes were made on the plate for inlet gas (Nitrogen) tube, condenser and thermometer respectively. The inlet gas tube was extended upto bottom of the reactor so that the nitrogen can bubble through the mixture. Only 50 mm Hg vacuum could be reached in this apparatus.

# Starting materials:



Adipic acid and propylene glycol were used as starting materials. 99% pure adipic acid (SDS make) having a melting point of 150°C and propylene glycol (analar grade, pfizer reagent) were used. Adipic acid and propylene glycol were taken as starting materials so that water analysis could be made which requires that unsaturation bonds be not present and so that liquid (noncrystalline) resins could be produced.

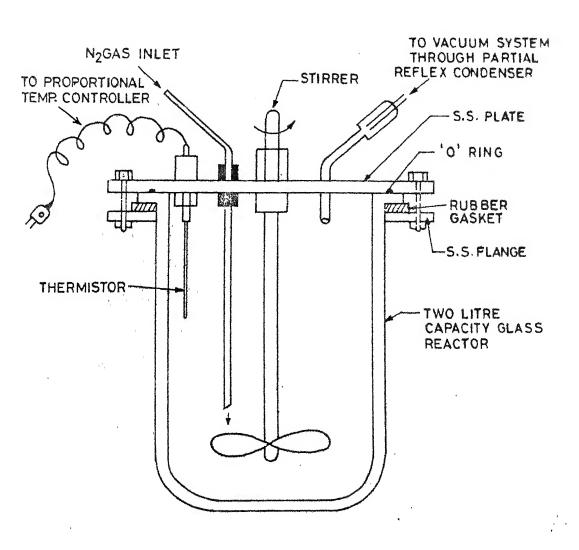


FIG.2 SKETCH OF THE REACTOR

## Procedure:

For the synthesis of polypropylene glycol adipate, adipic acid and propylene glycol were used as the starting materials. The starting materials were placed in a two litre capacity cylindrical glass reactor. The reaction mixture was heated by a heating mantle and the temperature was controlled by a proportional controller. Adipic acid and propylene glycol were taken in equimolar ratio. Propylene glycol was taken 5% in excess to prevent the loss of more volatile component from the reaction medium during the reaction. The reactants were preheated before they were placed together in the reactor. p-toluene sulfonic acid (0.015 equivalent/kg of reaction mixture) was added as a catalyst. The reaction mixture was heated with continous passage of a current of nitrogen. The heating was carried out for six hours at 180°C. A sample was taken out for analysis. Then, further heating was carried out at 150°C in a vacuum of 50 mm Hg for three more hours. A second sample was withdrawn from the reactor at the end of ninth hour. The temperature was again increased to nearly 190°C and the reaction was carried out for three more hours in a vacuum of 50 mm Hg. A third sample was taken out at the end of the reaction. The samples were analysed for acid number, hydroxyl number,

number average molecular weight from the end group analysis and the water content in the sample. The samples were also analysed in GPC (Gel permeation chromotography, waters Association, U.S.A.) for molecular weight distribution.

# Analytical procedure:

Determination of acid number: The acid number is defined as the number of mgs of KOH required to neutralize the carboxyl group in 1 gm.of acid. For the determination of acid number, a weighed sample of the resin was dissolved in a mixture of methanol, benzene and isopropanal and titrated against an alcoholic solution of KOH in the presence of phenolpthalein as indicator.

Acid number = 
$$\frac{a \times k \times 56.1}{b}$$

where

a = ml of KOH used in the titration.

k = normality of KOH

b = weight of the sample in gms.

<u>Determination of hydroxyl number</u>: The hydroxyl number is expressed in milligrams of KOH required to neutralise the acetic acid entering into the composition of acetylated product obtained from 1 gm. of substance under investigation.

An Acyetylation mixture was prepared by mixing 120 ml of acetic anhydride and 880 ml of anhydrous pyridine. A blank experiment was first carried out. For this, 10 ml of the acetylating mixture was titrated against a KOH solution in the presence of phenolphtalein. The aceylating mixture (20 ml) was added to the sample and was heated on a water bath for 15 minutes. After cooling, 25 ml of water was added, the mixture was cooled, and then titrated against KOH.

Hydroxyl number = 
$$\frac{(a+b-c) \times k \times 56.1}{d}$$

where

a = ml of KCH that were used to neutralise the acid

b = ml of KOH consumed in blank experiment

c = ml of KOH consumed in the working experiment

d = weight of the sample

<u>Determination of water</u>: Water was analysed by Karl-Fischer titration.

The conditions used for GPC analysis were as follows:

Columns employed:  $10^4 \text{ Å}$ ,  $10^3 \text{ Å}$ , 500 Å

Solvent : Chloroform

Elution rate: 1 ml/min

Calibration was done with Dodecyl mercaptan, and 2900, 4000, 9000, 50000 polystyrene standard.

Detector: Refractive index (401 Model), sensitivity 4X.

## Results and Discussion:

The analytical results of the resin are presented in Table 2. As the experiment proceeds, inspite of the partial condenser some ethylene glycol does vaporise. So the initial ratio of Glycol to Adipic acid will not be the proper ratio to use at all times. To avoid this difficulty, monitoring of the ethylene glycol in the condensate is to be done. In this work, to perform theoretical calculations it will be assumed that equilibrium has been achieved. This is justified by the following calculations:

Equilibrium constant 
$$\propto \frac{(\text{Acid number})(\text{Hydroxyl number})}{(\text{water})(\text{ester group})}$$

Further the number average molecular weight is given by half of sum of end groups or is proportional to half of sum of Acid number and Hydroxyl number.

Equilibrium constant 
$$\propto \frac{(\text{Acid number})(\text{Hydroxyl number})}{(\text{Water})(\text{Acid number} + \text{Hydroxyl number})}$$

These numbers for all the three resins are approximately the same. Hence it is reasonable to assume equilibrium has been reached. In theoretical calculations it was therefore assumed

Table 2

ANALYSIS OF RESINS

Resin number	Λcid number	Hydroxyl number	Water content wt.%	(Acid number+ Hydroxyl number)/2
1	<b>7</b> 7.5	60.2	1.20	68.8
2	41.3	40.5	0.62	40.9
3	23.8	20.8	0.36	22.3

that each resin was obtained from a resin whose initial glycol to acid ratio would be that which is consistent with the observations. Thus if  $\beta$  is the conversion of hydroxyl groups, and if R moles of glycol were taken per mole of acid, then

$$\frac{\text{Acid number x } 10^{-3}}{56.1} = \frac{2(1-R\beta)}{RM_G + M_{\Lambda} - 18R\beta}$$

$$\frac{\text{Hydroxyl number x } 10^{-3}}{56.1} = \frac{2R(1-\beta)}{RM_G + M_A - 18 R\beta}$$

From this R and  $\beta$  could be calculated. From results of Gandhi and Babu  $^2$ 

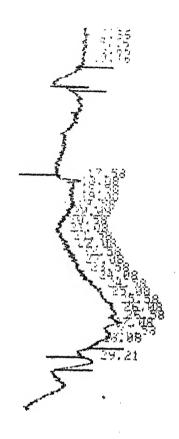
$$\overline{M}_{n} = (RM_{G} + M_{A})/(R+1-2\alpha)$$

$$PDI = (R+1-2\alpha)$$

$$\frac{M_{A}^{2}(1+R\beta) + 4\alpha M_{G} M_{A} + M_{G}^{2}(R+R^{2}\beta)}{(1-R\beta^{2})(RM_{G} + M_{A})^{2}}$$

The calculated values of R and  $\beta$  were then used to compute  $\overline{\underline{M}}$  and PDI for each resin. These are given in Table 3.

GPC results are presented in figures 3 to 9. Duplicate runs are also presented for comparison. Firstly the molecular weight can only be in increments of  $(M_G + M_A - 18)$  or approximately 200. While this does not pose any problem for high molecular weight samples, at low molecular weights it causes errors as



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CHAPT 0.50 CM/MIN

SOLDENT! CHLOROFORM CHROMATOGRAM OF SAMPLE 1

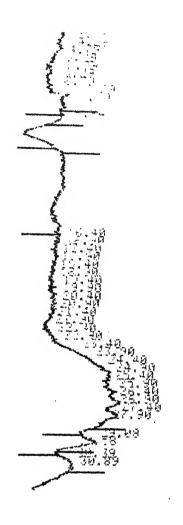
# · HL . # 1

# GPC DUHNTITHTION

RT	HAKEH	MOL WT	HE MW	
≟4.⊎8	2789500	0.149181E4	0.186987E4	F
14.58	7480040	0.114510E4	0.65147484	۶
5.08	10811800	0.875372E3	0.123510E5	F
25.Ea	14698400	0.6 <b>65</b> 786E3	8.319415E5	C
⊻ಕ.ಚಚ	17241600	0.50350064	1.34243465	F
76.58	1,7104100	0.378 LH	1.45209985	F
27.08	15492400	0.28335	. 545443E5	F
27.58	13336400	0.20947 : •	J. 533087E5	F
28.08	8486130	0.15%	11,1 47523E5	F
39.45	1055780	0.12:4	.369162E4	L

MU-HILL MT-AUG Z-ANG NIS-AUG

DISPERSITY 0.14428281 INTRINSIC USSCOSITY 0.5139328-3



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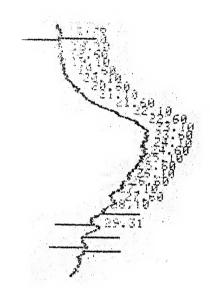
CHART 0.50 CM-MIN MUN #6 SOLVENT: CHLOROFORM

SOC QUANTITATION CHROMATOGRAM OF SAMPLE 1 (RAPSAT)

ET	HHEA	MOL AT	4.74	
23.90	1969820	0.163948E4	0.12014964	F
54.40	8599450	0.126030E4	0.682333E4	F
24.90	14814600	0.964931E3	0.153530E5	F
25,40	15102600	0.735077E3	0.205456E5	F
25.30	14222300	0.557163E3	0.25526265	F
26.40	15881600	0.419778E3	0.378333E5	F
25.90	17535200	0.314030E3	0.55839265	F
a?.4₫	13175200	0.2332 <b>35E3</b>	0.564932E5	F
37.90	12913200	0.171816E3	0.75157165	F
33.38	4762990	0.127028E3	0.374955E5	1

0.358074E3 0.550177E3 0.779513E3 0.550070E3 ハリーみひら

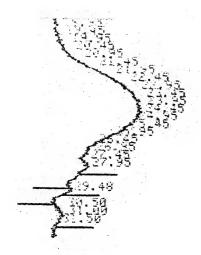
DISPERSITY 0.153648E1 INTRINSIC DISCOSITY 0.549960E-3



DISFERSITY 0.220973E1

INTRINSIC DISCOSITY 0.197295E-2

-59, 6, 1982 15:19:51 CHART 0.50 CM/MIN RUN #3 COLUMN: 104A, 103A, 500A CHLC #1 SOLVENT: CHLOROFORM 101 SPC, QUANTITATION CHROMATOGRAM OF SAMPLE 1 HREA MOL WT A-MW Q0. 10 125610 0,114217E5 0.109974E2 F 20.50 3456470 0.884829E4 F 0.39063763 21.19 7335750 0.486275E4 0.10544964 444 11.60 0.532613E4 14006100 9.262969E4 12,14 23847400 0.413358E4 9.576918E4 22.59 33115500 0.320472E4 0.103333E5 F 38113500 FF 0.248096E4 0.15362465 13.60 0.191670E4 37547400 0.19641725 34.10 0.147639E4 F 35019300 0.23720965 1.1 24.59 33957799 0.299738E5 0.113291E4 มีรังนี้ ติ 38612769 0.865839E3 0.353561E5 25.60 26656588 1 0.658403E3 0.395661E5 18.10 21558100 0.497771E3 0.433092E5 25.59 16953800 0.453289E5 F 0.374917E3 23.10 0.409399E5 F 11424700 0.279060E3 F 17:58 8675560 0.419955E5 0.206583E3 0.30295965 F 4593840 13.18 0.15163223 39.42 396969 0.123839E3 0.247149E4 MU-405 9.893216E3 MI-AUG 8.197377E4 T-AUG 0.337396E4 S-AUG 0.197335E4



AUG. 6, 1982 15:58:16 CHART 0.50 CM/MIN
COLUMN: 10<sup>4</sup>A, 10<sup>8</sup>A, 500A SOLVENT: CHLOROFORM

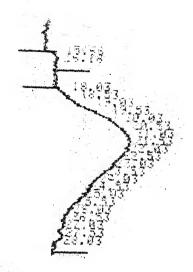
CHROMATOGRAM OF SAMPLE 2 (REPEAT)

RT	AREA	MOL WT	9/MD	
20.45	158395	0.954897E4	0.165876E2	F
20.95	4073789	0.740545E4	0.550105E3	F
21,45	10719900	0.574790E4	0.186501E4	F
21.95	19950800	0.446005E4	0.447322E4	F
22.45	28000400	0.345954E4	0.809367E4	F
22.55	34116800	0.267959E4	0.127320E5	F
23,45	38111700	0.207152E4	0.183979E5	F
23.95	40196000	9.159719E4	0.251666E5	F
24.45	40118600	0.122699E4	0.326967E5	F
24.95	37302900	0.939086E3	0.397225E5	F
25,45	31698000	0.715140E3	0.443241E5	F
25.95	23300100	0.541717E3	0.430115E5	F
26.45	13676400	0.407839E3	0.335338E5	F
26.95	6906420	0.304837E3	0.22656165	F
27.45	3199210	0.226244E3	0.141405E5	F
27.95	3902780	0.166532E3	0.234356E5	F
28.35	223140	0.129501E3	0.172307E4	L
				18. T

NO-AUG 0.10279164 WT-AUG 0.19137264 2-AUG 0.30428764 UIS-AUG 0.19130764

GPC QUANTITATION

DISPERSITY 0.186175E1 INTRINSIC VISCOSITY 0.191288E-2



AUG. 6/ 1982 | 13:51/23

COLUMN: 104A, 103A, 500A°

CHART 0.50 CH/MIN RUN #1 SOLUENT: CHLOROFORM · Chilly #1

1" 233		100	1.	1.1.1	***	*		A.,	7	٣	P 11	
13.0	an'	w	J 1	414	3.	ì.	4	<b>∤</b> →	1	1	1.11	

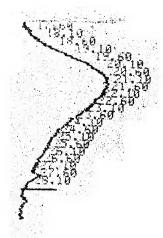
# CHROMATOGRAM OF SAMPLE 3

RT AREA	MOL WT	A. MU
18.03 2307530	0.338070E5	0.68255982 F
18.53 7515030	0.258635E5	
19.03 14585200	0.198699E5	0.290565E3 F 0.734034E3 F
19153 24788788	0.15317965	
20.03 33990460	0.118407E5	0.287064F4 F
20.53 40233300	0.917001E4	0.438748E4 F
21.03 44055300	0.711180E4	0.161828E4 F 0.287064E4 F 0.438748E4 F 0.619467E4 F
21.53 45265300	0.55205264	0.819946E4 F
32.03 43476800	0.428386E4	0.101489E5 F
22.53 39075000	0.332171E4	
33.03 35479400	0.257229E4	0.137929E5 F
23.53 29617400	0.198809E4	0.148974E5 F
24.03 24658900	0.153194E4	0.160965E5 F
24.53 21838100	0.117622E4	0.185663E5 F
25.03 1800 <b>2400</b>	0.899379E3	0.200164E5 F
25.53 13040400	0.684319E3	0.190560E5 F
36.03 9581830	0.517986E3	0.184982E5 F
26.53 7321160	0.389481E3	0.187972£5 F
27.83 6021800	0.290856E3	0.207037E5 F
27.53 5625250	0.215565E3	0.207037E5 F 0.260953E5 F
28.03 2418760	0.158486E3	0.152616E5 F
28.43 737973.	0.123017E3	0.599895E4 EL
man and a second of the second	W - 2 1 - 2 - 2 - 2 - 2 - 2 - 2 - 2 - 2 -	

40-AUG 46.184855E4 0.605260E4 MT-AUG

2-406 0.115002E5 015-406 0.605079E4

013P2#81TY 0.327424E1 INTRINSIC VISCOSITY 0.605076E-2



AUG. 6, 1982 14.34:43 CHART 9.50 CM MIN COLUMN: 10 A, 10 A, 500 A RUN #2 CALC #4 SULUENT: CHLOROPORM 10: CHROMATOGRAM OF GPC QUANTITATION SAMPLE 3 (REPEAT) AREA RI MOL HT 4/ Mu 1203640 17.68 0.427147E5 0.28178562 F 18.10 5100378 0.325497E5 0.156694E3 F 19.60 11682900 0.249190E5 0.468835E3 F 19.18 21465700 0.191536E5 0.112071E4 F 19.60 32877500 0.147705E5 0.22258884 20.19 42159800 0.114217E5 0.36912084 20.60 49184000 0.88482984 0.55585884 21.19 51758600 9.754196E4 0.686275E4 21.60 50590500 0.532613E4 0.94985464 9.115601E5 22, 19 47785000 0.413358E4 12.60 43337190 0.320472E4 0.135228E5 0.248096E4 23.10 32737400 3.60 31247300 0.152108E5 0.191679E4 9.163026E5 34.10 25894400 0.147630E4 0.175400ES 20909200 0.113291E4 9.184561E5 24.60 0.19786865 F A.865839E3 25.19 17132200 25.80 0.658403E3 F 14934800 0.226833E5 25, 10 0.242364E5 0.497771E3 12064200 0.374017E3 ·0.246161E5 28.50 9286868 27.19 0.24221365 6753220 0.279060E3 0.206583E3 27.60 8320240 0.40275565 0,228201E5 3460270 23,10 0.151632E3 368997 0.123839E3 0.297965E4 23, 42 NO-AUG 0.179039E4

CISPERSITY 0.362349E1 INTRINSIC WISCOSITY 0.648535E-2 GPC takes the curve to be continuous. This can be avoided only if the resolution is improved by use of other columns. As they were not available, the analysis could not be improved. The results of GPC are also presented in Table 3. Considering the difficulty with resolution, the disagreement between GPC results and others can not be commented upon.

 $\overline{\mathbb{M}}_n$  can also be calculated from analytical results. It is given by

$$\overline{M}_{n} = \frac{\text{Equivalent weight of KOH x 10}^3}{(\Lambda \text{cid number + hydroxyl number})/2}$$

These results are also presented in Table 3. The agreement between theory and experiment can be considered satisfactory.

It can be concluded that the experimental set up is to be modified to get better vacuum for making high molecular weight resins and that columns have to be added to GPC to get better resolution. Monitoring of glycol concentration in the condensate is also necessary. For the given set up the agreement between theory and experiment is satisfactory.

Table 3

COMPARISON BETWEEN THEORETICAL AND EXFLANABLE RESULTS

Resin number	M ^haly <b>tic</b> el	M	Theory PDI	M n	GPC PDI
1	814	728	3.76	~350	1.7
2	1365	1316	4.40	~890	2.2
3	2513	2665	4.40	~1790	3.6

### CHAPTER 5

#### CONCLUSIONS

It was shown that the MWD for reversible as well as irreversible step polymerisation with unequal reactivities are identical if it is assumed that in a given species all internal arrangements are equally probable.

An algorithm given by Vimala and Nath was used to solve the linear simultaneous partial differential equations describing simultaneous diffusion and polycondensation and the results compared well with the exact solution available.

The experimental setup designed to make polyesters has to be modified to get better vacuum for making high molecular weight resins. Some additional columns have to be added to GPC to get better resolution. Monitoring of glycol and water in the condensate may be necessary to calculate MWD.

### REFERENCES

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